

**Mark scheme for Support Worksheet – Topic E,
Worksheet 3**

- 1 **a** For the $1 M_{\odot}$ mass star the stages are red giant, planetary nebula and white dwarf. [1]
- b** For the $1 M_{\odot}$ mass star the stages are red supergiant, supernova and most likely a neutron star. [1]
- 2 Since $L \propto M^{3.5}$ we have that $L = L_{\odot} 3^{3.5} = 46.8 L_{\odot} \approx 47 L_{\odot}$ [1]
- 3 This is the highest mass a white dwarf can have (and equals about $1.4 M_{\odot}$). [1]
- 4 This is the highest mass a neutron star can have (and equals about $3 M_{\odot}$). [1]
- 5 A neutron star that rotates about its axis with a magnetic field that has a different direction from that of the axis of rotation. [1]
- 6 Because pulsars radiate radio waves and not visible light. [1]
- 7 Distant galaxies move away from each other with a speed proportional to their separation. [1]
- 8 Because galaxies that are near each other attract each other gravitationally and may move towards each other. [1]
- 9 $\frac{\Delta\lambda}{\lambda} = \frac{v}{c} \Rightarrow v = \frac{\Delta\lambda}{\lambda} c$; hence $v = \frac{680 - 656}{656} \times 3 \times 10^8 = 1.1 \times 10^7 \text{ m s}^{-1}$ [2]
- 10 $\frac{\Delta\lambda}{\lambda} = \frac{v}{c} \Rightarrow v = \frac{\Delta\lambda}{\lambda} c$; hence
 $v = \frac{670 - 656}{656} \times 3 \times 10^8 = 6.4 \times 10^6 \text{ m s}^{-1} = 6.4 \times 10^3 \text{ km s}^{-1}$; therefore
 $d = \frac{v}{H} = \frac{6.4 \times 10^3}{73} = 87.67 \approx 88 \text{ Mpc}$ [3]
- 11 $\frac{1}{H} = \frac{1}{73 \text{ km s}^{-1} \text{ Mpc}^{-1}} = \frac{1}{73} \frac{10^6 \times 3.26 \times 9.46 \times 10^{15}}{10^3 \times 365 \times 24 \times 3600} = 1.34 \times 10^{10} \text{ yr}$, i.e. about 13 billion years. [1]
- 12 Assume that galaxies move away from each other at the present speed of $v = Hd$ where d is their present separation; then $v = \frac{d}{T}$ where T is the age of the universe; combining gives $T = \frac{1}{H}$. [3]